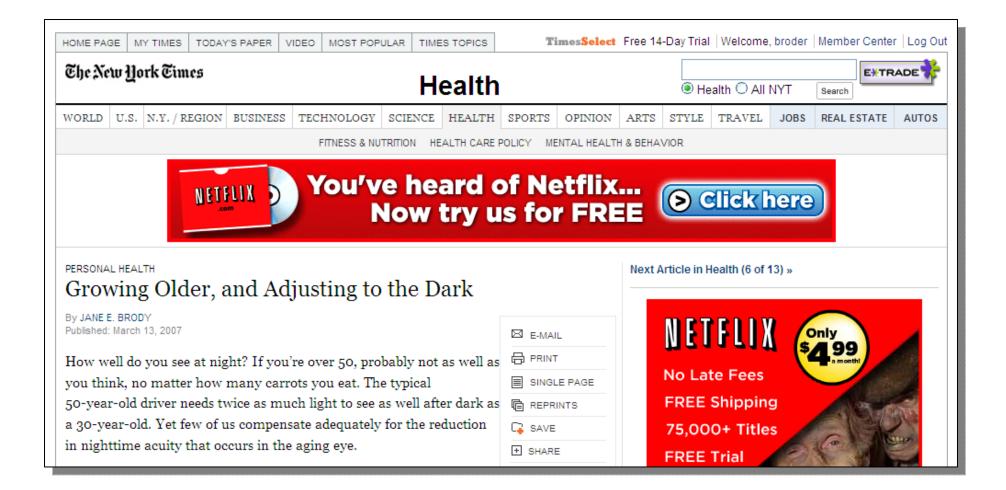


Display Advertising Impressions





Display Advertising

- Contracts purchased in advance
- Typically guarantee number of impressions
- Set types of eligible opportunities
 - 30-40 year old males
 - Californians on auto pages
- Supply random
- Excess sold on spot market
- Two main problems
 - Cream-skimming
 - Orphan categories

Objective Function Requirements

- Flexibility in serving
- Spot revenue
- Insuring quality of booked campaigns
- Risk of under and over delivery
- Handling orphan inventory categories
- Scarcity pricing



Objective Function

Serving Representativeness

Lost Spot Revenue

$$\min \Phi = \gamma \left\{ \frac{1}{2} \sum_{j} V^{j} Y^{j} \sum_{i \in B^{j}} \frac{\sum_{k \in B^{j}} x_{k}}{x_{i}} \left\{ \frac{x_{i}}{\sum_{k \in B_{j}} x_{k}} - \frac{y_{i}^{j}}{Y^{j}} \right\}^{2} \right\} - \sum_{i} [r_{i} z_{i}]$$
$$x_{i} \geq \sum_{j \mid i \in B^{j}} y_{i}^{j} \qquad Y^{j} = \sum_{i \in B^{j}} y_{i}^{j}$$

Y^j: Requested demand for contract j B^j: Eligible impressions for contract j x_i : Available supply for impression i

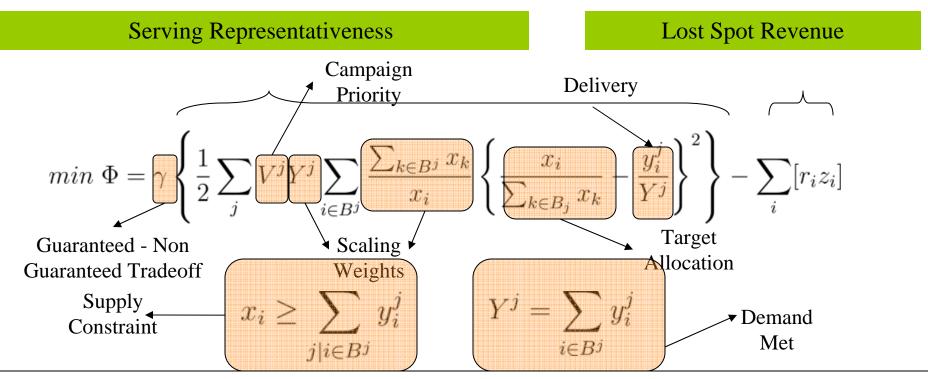
 r_i : Opportunity cost for impression i

z_i : Slack for impression i

y^j_i: Amount of impression i supply allocated to contract j



Objective Function



Y^j: Requested demand for contract j B^j: Eligible impressions for contract j x_i : Available supply for impression i r_i : Opportunity cost for impression i

z_i : Slack for impression i

yⁱ_i: Amount of impression i supply allocated to contract j

Theorem

- There is an implementation using randomized bidding into an exchanges
- Distribution of bids is uniform
- Bidding distributions do not depend on type of inventory
- Bidding distributions have closed forms
- Can approximate without pricing orphaned categories!

Key Innovations

- Entire system designed to meet overall objective
- Fine-grained targeting
 - Forecasting, admission control and serving
- Integrated pricing and allocation
 - Price based on expected allocation
- Business knobs control all trade-offs



 Inventory allocation across guaranteed and spot demand

- Unified marketplace

• User modeling

Forward Looking Innovations



Thank you!

