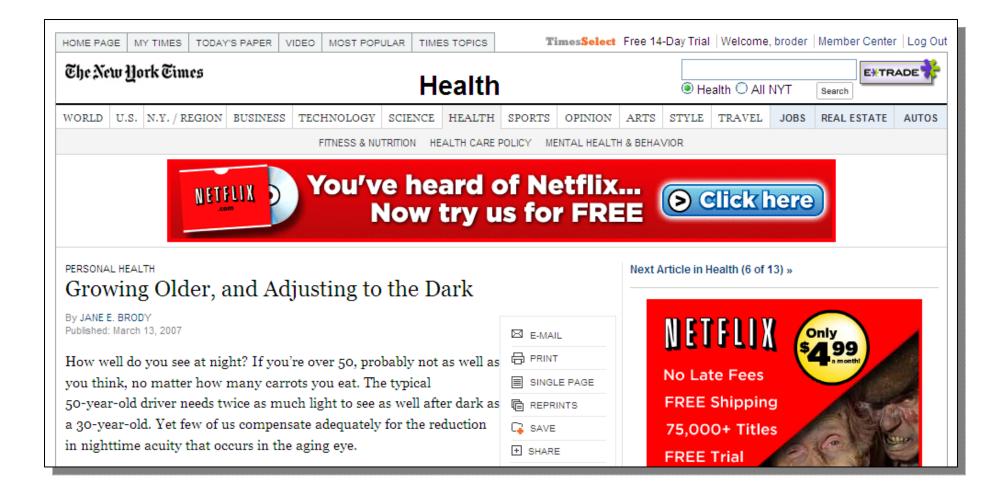


# **Display Advertising Impressions**





# **Display Advertising**

- Contracts purchased in advance
- Typically guarantee number of impressions
- Set types of eligible opportunities
  - 30-40 year old males
  - Californians on auto pages
- Supply random
- Excess sold on spot market
- Two main problems
  - Cream-skimming
  - Orphan categories

# **Objective Function Requirements**

- Flexibility in serving
- Spot revenue
- Insuring quality of booked campaigns
- Risk of under and over delivery
- Handling orphan inventory categories
- Scarcity pricing



#### **Objective Function**

Serving Representativeness

Lost Spot Revenue

$$\min \Phi = \gamma \left\{ \frac{1}{2} \sum_{j} V^{j} Y^{j} \sum_{i \in B^{j}} \frac{\sum_{k \in B^{j}} x_{k}}{x_{i}} \left\{ \frac{x_{i}}{\sum_{k \in B_{j}} x_{k}} - \frac{y_{i}^{j}}{Y^{j}} \right\}^{2} \right\} - \sum_{i} [r_{i} z_{i}]$$
$$x_{i} \geq \sum_{j \mid i \in B^{j}} y_{i}^{j} \qquad Y^{j} = \sum_{i \in B^{j}} y_{i}^{j}$$

Y<sup>j</sup>: Requested demand for contract j B<sup>j</sup>: Eligible impressions for contract j  $x_i$ : Available supply for impression i

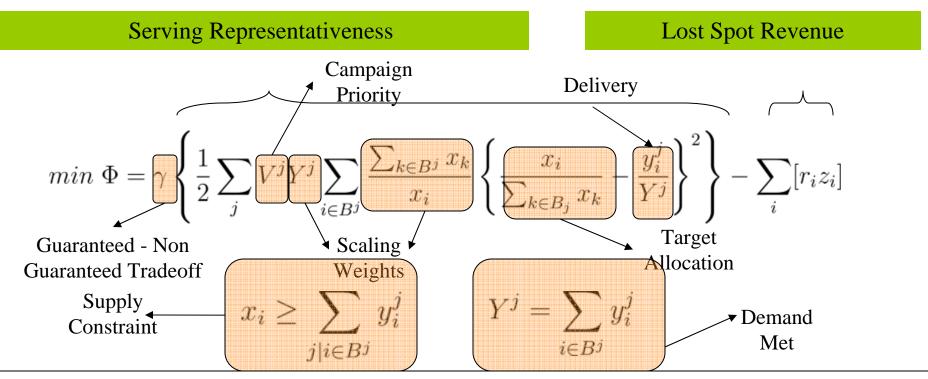
 $r_i$ : Opportunity cost for impression i

z<sub>i</sub> : Slack for impression i

y<sup>j</sup><sub>i</sub>: Amount of impression i supply allocated to contract j



## **Objective Function**



Y<sup>j</sup>: Requested demand for contract j B<sup>j</sup>: Eligible impressions for contract j  $x_i$ : Available supply for impression i  $r_i$ : Opportunity cost for impression i

z<sub>i</sub> : Slack for impression i

y<sup>i</sup><sub>i</sub>: Amount of impression i supply allocated to contract j

#### Theorem

- There is an implementation using randomized bidding into an exchanges
- Distribution of bids is uniform
- Bidding distributions do not depend on type of inventory
- Bidding distributions have closed forms
- Can approximate without pricing orphaned categories!

#### **Key Innovations**

- Entire system designed to meet overall objective
- Fine-grained targeting
  - Forecasting, admission control and serving
- Integrated pricing and allocation
  - Price based on expected allocation
- Business knobs control all trade-offs



 Inventory allocation across guaranteed and spot demand

- Unified marketplace

• User modeling

Forward Looking Innovations



# Thank you!

